# Package: pprof (via r-universe)

December 13, 2024

Type Package

**Title** Risk-adjusted Models, Standardized Measure Calculation, Hypothesis Testing and Visualization for Provider Profiling

**Version** 1.0.1 **Date** 2024-11-18

Description Implements linear and generalized linear models for provider profiling, incorporating both fixed and random effects. For large-scale providers, the linear profiled-based method and the SerBIN method for binary data reduce the computational burden. Provides post-modeling features, such as indirect and direct standardization measures, hypothesis testing, confidence intervals, and post-estimation visualization. For more information, see Wu et al. (2022) <doi:10.1002/sim.9387>.

License MIT + file LICENSE

LazyData true

**Imports** Rcpp, RcppParallel, stats, caret, olsrr, pROC, poibin, dplyr, ggplot2, Matrix, lme4, magrittr, scales, tibble, rlang

LinkingTo Rcpp, RcppArmadillo, RcppParallel

**Depends** R (>= 4.1.0)

**Suggests** knitr, rmarkdown, testthat (>= 3.0.0)

VignetteBuilder knitr RoxygenNote 7.3.1

URL https://github.com/UM-KevinHe/pprof

**Encoding UTF-8** 

SystemRequirements GNU make

**Roxygen** list(markdown = TRUE)

Config/testthat/edition 3

Config/pak/sysreqs cmake make libicu-dev zlib1g-dev

Repository https://um-kevinhe.r-universe.dev

2 bar\_plot

RemoteUrl https://github.com/um-kevinhe/pprof

RemoteRef HEAD

 $\textbf{RemoteSha} \ 7b0f6a742e931d19a5195da2fd0a3f9d234ddf12$ 

# **Contents**

bar_p	olot	Get a bar plot for flagging percentage overall and stra provider sizes	tified by
Index			39
	iesi.iogis_ie		31
	SM_output.logis_fe		29
	SM_output.linear_re		28
	SM_output.linear_fe		26
	*		
	•		
	•		
		·	
	•		
	confint.linear_fe		6
	-		
	par_piot		

# Description

Generate a bar plot for flagging percentage.

bar\_plot 3

#### Usage

```
bar_plot(
  flag_df,
  group_num = 4,
  bar_colors = c("#66c2a5", "#fc8d62", "#8da0cb"),
  bar_width = 0.7,
  label_color = "black",
  label_size = 4
)
```

#### **Arguments**

flag_df	a data frame from test function containing the flag of each provider.
group_num	number of groups into which providers are divided based on their sample sizes. The default is 4.
bar_colors	a vector of colors used to fill the bars representing the categories. The default is $c(\#66c2a5\%, \#fc8d62\%, \#8da0cb\%)$ .
bar_width	width of the bars in the bar chart. The default is 0.7.
label_color	color of the text labels inside the bars. The default is "black".
label_size	size of the text labels inside the bars. The default is 4.

#### **Details**

This function generates a bar chart to visualize the percentage of flagging results based on provider sizes. The input data frame test\_df must be the output from package pprof's test function. Providers are grouped into a specified number of groups (group\_num) based on their sample sizes, where the number of providers are approximately equal across groups. An additional "overall" group is included to show the flagging results across all providers.

# Value

A ggplot object representing the bar chart of flagging results.

#### See Also

```
test.linear_fe, test.linear_re, test.logis_fe
```

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_linear <- linear_fe(Y = outcome, Z = covar, ID = ID)
test_linear <- test(fit_linear)
bar_plot(test_linear)
data(ExampleDataBinary)</pre>
```

4 caterpillar\_plot

caterpillar\_plot

Get a caterpillar plot to display confidence intervals for standardized measures

### **Description**

Generate a caterpillar plot for standardized measures from different models using a provided CI dataframe.

#### Usage

```
caterpillar_plot(
   CI,
   point_size = 2,
   point_color = "#475569",
   refline_value = NULL,
   refline_color = "#64748b",
   refline_size = 1,
   refline_type = "dashed",
   errorbar_width = 0,
   errorbar_size = 0.5,
   errorbar_alpha = 0.5,
   errorbar_color = "#94a3b8",
   use_flag = FALSE,
   flag_color = c("#E69F00", "#56B4E9", "#009E73")
)
```

#### **Arguments**

CI	a dataframe from confint function containing the standardized measure values, along with their confidence intervals lower and upper bounds.
point_size	size of the points in the caterpillar plot. The default value is 2.
point_color	color of the points in the plot. The default value is "#475569".
refline_value	value of the horizontal reference line, for which the standardized measures are compared. The default value is NULL.
refline_color	color of the reference line. The default value is "#64748b".
refline_size	size of the reference line. The default value is 1.
refline_type	line type for the reference line. The default value is "dashed".

caterpillar\_plot 5

errorbar\_width the width of the error bars (horizontal ends of the CI bars). The default value is 0.

errorbar\_size the thickness of the error bars. The default value is 0.5.

errorbar\_alpha transparency level for the error bars. A value between 0 and 1, where 0 is completely transparent and 1 is fully opaque. The default value is 0.5.

errorbar\_color color of the error bars. The default value is "#94a3b8".

use\_flag logical; if TRUE, the error bars are colored to show providers' flags based on their performance. The default is FALSE.

flag\_color vector of colors used for flagging providers when use\_flag = TRUE. The default value is c("#E69F00", "#56B4E9", "#009E73").

#### **Details**

This function creates a caterpillar plot to visualize the standardized measures (indirect or direct). The input CI must be a dataframe output from package pprof's confint function. Each provider's standardized measure value is represented as a point, and a reference line is shown at the value specified by refline\_value (default is NULL). If refline\_value is not specified, for linear FE or RE models with indirect or direct standardized differences, it will be set to 0; for logistic FE models with indirect or direct ratios, it will be set to 1; and for logistic FE with indirect or direct rates, it will be set to the population rate, which represents the average rate across all observations.

Confidence intervals (CI) are displayed as error bars: for alternative = "two.sided", two-sided confidence intervals are shown; for alternative = "greater", error bars extend from the lower bound to the standardized measure values; and for alternative = "less", they extend from the standardized measure values to the upper bound. For cases where one side of the confidence interval is infinite, that side only extends to the standardized measure. For example, in a logistic fixed effect model, if a provider has all 0s or all 1s, one side of the confidence interval will be infinite.

When use\_flag = TRUE, the plot will use colors specified by flag\_color to show the flags of providers. Each error bar will be colored to reflect the flag, making it easy to identify providers with different performance levels. When use\_flag = FALSE, all error bars will have the same color, specified by errorbar\_color. This provides a simpler visualization without flagging individual providers.

#### Value

A ggplot object which is a caterpillar plot for the standardized measures.

# See Also

```
confint.linear_fe, confint.linear_re, confint.logis_fe
```

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_linear <- linear_fe(Y = outcome, Z = covar, ID = ID)
CI_linear <- confint(fit_linear)</pre>
```

6 confint.linear\_fe

confint.linear\_fe

Get confidence intervals for provider effects or standardized measures from a fitted linear\_fe object

#### **Description**

Provide confidence intervals for provider effects or standardized measures from from a fixed effect linear model.

#### Usage

```
## S3 method for class 'linear_fe'
confint(
    fit,
    parm,
    level = 0.95,
    option = "SM",
    stdz = "indirect",
    null = "median",
    alternative = "two.sided",
    ...
)
```

#### **Arguments**

fit a model fitted from linear\_fe.

parm specify a subset of providers for which confidence intervals are given. By de-

fault, all providers are included. The class of parm should match the class of the

provider IDs.

level the confidence level. The default value is 0.95.

option a character string specifying whether the confidence intervals should be pro-

vided for provider effects or standardized measures:

• "gamma" provider effect (only supports "two.sided" confidence interval).

• "SM" standardized measures.

confint.linear\_re 7

stdz	a character string or a vector specifying the standardization method if option includes "SM". See stdz argument in SM_output.linear_fe.
null	a character string or a number specifying the population norm for calculating standardized measures if option includes "SM". See null argument in SM_output.linear_fe.
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater", or "less". Note that "gamma" for argument option only supports "two.sided".
	additional arguments that can be passed to the function.

#### Value

A list of data frames containing the confidence intervals based on the values of option and stdz.

CI.gamma Confidence intervals for provider effects if option includes "gamma".

CI.indirect Confidence intervals for indirect standardized differences if option includes "SM" and stdz includes "indirect".

CI.direct Confidence intervals for direct standardized differences if option includes "SM" and stdz includes "direct".

# Examples

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_linear <- linear_fe(Y = outcome, Z = covar, ID = ID)
confint(fit_linear)</pre>
```

confint.linear\_re Get confidence intervals for provider effects or standardized measures from a fitted linear\_re object

#### **Description**

Provide confidence intervals for provider effects or standardized measures from a random effect linear model.

```
## S3 method for class 'linear_re'
confint(
   fit,
   parm,
   level = 0.95,
   option = "SM",
```

8 confint.linear\_re

```
stdz = "indirect",
alternative = "two.sided",
...
)
```

#### **Arguments**

fit

specify a subset of providers for which confidence intervals are given. By default, all providers are included. The class of parm should match the class of the provider IDs.

level the confidence level. The default value is 0.95.

option a character string specifying whether the confidence intervals should be provided for provider effects or standardized measures:

• "alpha" provider effect.
• "SM" standardized measures.

stdz a character string or a vector specifying the standardization method if option

includes "SM". See stdz argument in SM\_output.linear\_re.

alternative a character string specifying the alternative hypothesis, must be one of "two.sided"

(default), "greater", or "less". Note that "alpha" for argument option only

supports "two.sided".

... additional arguments that can be passed to the function.

a model fitted from linear\_re.

#### Value

A list of data frames containing the confidence intervals based on the values of option and stdz.

CI.alpha Confidence intervals for provider effects if option includes "alpha".

CI.indirect Confidence intervals for indirect standardized differences if option includes

"SM" and stdz includes "indirect".

CI.direct Confidence intervals for direct standardized differences if option includes "SM"

and stdz includes "direct".

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
ID <- ExampleDataLinear$ID
covar <- ExampleDataLinear$Z
fit_re <- linear_re(Y = outcome, Z = covar, ID = ID)
confint(fit_re)</pre>
```

confint.logis\_fe 9

 $confint.logis\_fe$ 

Get confidence intervals for provider effects or standardized measures from a fitted logis\_fe object

#### **Description**

Provide confidence intervals for provider effects or standardized measures from a fixed effect logistic model.

#### Usage

```
## $3 method for class 'logis_fe'
confint(
    fit,
    parm,
    level = 0.95,
    test = "exact",
    option = "SM",
    stdz = "indirect",
    null = "median",
    measure = c("rate", "ratio"),
    alternative = "two.sided",
    ...
)
```

#### **Arguments**

stdz

fit a model fitted from logis\_fe.

parm specify a subset of providers for which confidence intervals are given. By de-

fault, all providers are included. The class of parm should match the class of the

provider IDs.

level the confidence level. The default value is 0.95.

test a character string specifying the type of testing method. The default is "exact".

• "exact" exact test.

• "wald" wald test.

• "score" score test.

option a character string specifying whether the confidence intervals should be pro-

vided for provider effects or standardized measures:

• "gamma" provider effect.

• "SM" standardized measures.

a character string or a vector specifying the standardization method if option = "SM". See stdz argument in SM\_output.logis\_fe.

null a character string or a number defining the population norm if option = "SM".

10 data\_check

measure

a character string or a vector indicating whether the output measure is "ratio" or "rate" if option = "SM". Both "rate" and "ratio" will be provided by default.

- "rate" output the standardized rate. The "rate" has been restricted to 0% 100%.
- "ratio" output the standardized ratio.
- c("ratio", "rate") output both the standardized rate and ratio.

alternative

a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater", or "less". Note that "gamma" for argument option only supports "two.sided".

. . additional arguments that can be passed to the function.

#### **Details**

The wald test is invalid for extreme providers (i.e. when provider effect goes to infinity). We suggest using score or exact test to generate confidence intervals.

#### Value

A dataframe (option = "gamma") or a list of data frames (option = "SM") containing the point estimate, and lower and upper bounds of the estimate.

### **Examples**

```
data(ExampleDataBinary)
outcome = ExampleDataBinary$Y
covar = ExampleDataBinary$Z
ID = ExampleDataBinary$ID
fit_fe <- logis_fe(Y = outcome, Z = covar, ID = ID, message = FALSE)
confint(fit_fe, option = "gamma")
confint(fit_fe, option = "SM")</pre>
```

data\_check

Data quality check function

### **Description**

Conduct data quality check including checking missingness, variation, correlation and VIF of variables.

```
data_check(Y, Z, ID)
```

ecls\_data 11

#### **Arguments**

e.
e

Z a matrix or data frame representing covariates.

ID a numeric vector representing the provider identifier.

#### **Details**

The function performs the following checks:

- Missingness: Checks for any missing values in the dataset and provides a summary of missing data.
- Variation: Identifies covariates with zero or near-zero variance which might affect model stability.
- Correlation: Analyzes pairwise correlation among covariates and highlights highly correlated pairs.
- VIF: Computes the Variable Inflation Factors to identify covariates with potential multicollinearity issues.

If issues arise when using the model functions logis\_fe, linear\_fe and linear\_re, this function can be called for data quality checking purposes.

#### Value

No return value, called for side effects.

#### **Examples**

```
data(ExampleDataBinary)
outcome = ExampleDataBinary$Y
covar = ExampleDataBinary$Z
ID = ExampleDataBinary$ID
data_check(outcome, covar, ID)
```

ecls\_data

Early Childhood Longitudinal Study Dataset

### **Description**

The Early Childhood Longitudinal Study (ECLS) dataset tracks more than 18,000 children from kindergarten through fifth grade, providing comprehensive student-level information. See Tourangeau et al. (2015) for details.

```
data(ecls_data)
```

12 ecls\_data

#### **Format**

A data frame with 9,101 observations, including:

Child\_ID Unique identifier for each child in the dataset.

**School ID** Identifier for each school in the dataset.

Math\_Score Continuous variable representing the consolidated math proficiency score.

**Income** Household income, categorized into 18 ordinal levels, from \$5,000 or less to \$200,000 or more. Treated as a continuous variable in the analysis.

**Child\_Sex** Binary variable indicating the gender of each student.

#### **Details**

The dataset includes fifth-grade cross-sectional data, focusing on students' mathematical assessment scores as the primary outcome measure. The mathematical assessment covers 18 topics such as number sense, properties, operations, measurement, geometry, data analysis, and algebra. These items evaluate students' competencies in conceptual knowledge, procedural knowledge, and problem-solving, consolidated into a single "Math score." A higher score indicates greater proficiency. The primary predictors are household income and gender, where gender is a categorical variable. Household income is categorized into 18 ordinal levels, ranging from \$5,000 or less (level 1) to \$200,000 or more (level 18). In the analysis, the income variable is treated as a continuous variable. The dataset removes all records with missing values and consists of 9,101 complete observations from 2,275 schools.

#### Source

Available at the following website: https://nces.ed.gov/ecls/.

#### References

Tourangeau, K., Nord, C., Lê, T., Sorongon, A. G., Hagedorn, M. C., Daly, P., & Najarian, M. (2015). Early Childhood Longitudinal Study, Kindergarten Class of 2010-11 (ECLS-K:2011): User's manual for the ECLS-K:2011 kindergarten data file and electronic codebook, public version (NCES 2015-074). National Center for Education Statistics.

```
data(ecls_data)
formula_FE <- as.formula("Math_Score ~ Income + id(School_ID) + Child_Sex")
fit_FE <- linear_fe(formula = formula_FE, data = ecls_data)

formula_RE <- as.formula("Math_Score ~ Income + (1|School_ID) + Child_Sex")
fit_RE <- linear_re(formula = formula_RE, data = ecls_data)</pre>
```

ExampleDataBinary 13

ExampleDataBinary

Example data with binary outcomes

# Description

A simulated data set containing 7994 observations, 5 continuous covariates and 100 providers.

### Usage

```
data(ExampleDataBinary)
```

#### **Format**

A list containing the following elements:

- Y a vector representing binary outcomes with 0 or 1. Generated from a Bernoulli distribution with the probability of success  $(\mu)$ , which is determined by applying the logistic function to the linear combination of provider effects and covariates.
- **ID** a vector representing identifier for each provider. The number of individuals per provider is generated from a Poisson distribution with mean 80, with a minimum value of 11.
- **Z** a data frame containing 5 continuous variables. Generated from a multivariate normal distribution, where the mean is calculated as  $(\gamma_i \mu_\gamma) \cdot \rho/\sigma_\gamma$  with  $\mu_\gamma = \log(4/11)$  and  $\sigma_\gamma = 0.4$ , and the correlation between covariates and provider effects is 0.1.

#### **Examples**

```
data(ExampleDataBinary)
head(ExampleDataBinary$Y)
head(ExampleDataBinary$ID)
head(ExampleDataBinary$Z)
```

ExampleDataLinear

Example data with continuous outcomes

#### **Description**

A simulated data set containing 7901 observations, 5 continuous covariates and 100 providers.

```
data(ExampleDataLinear)
```

14 linear\_fe

#### **Format**

A list containing the following elements:

Y a vector representing continuous outcomes. Generated as a linear combination of provider-specific effects, covariates, and a random error term  $(\epsilon)$ , where  $\epsilon$  follows a normal distribution with mean 0 and standard deviation 1.

- **ID** a vector representing identifier for each provider. The number of individuals per provider is generated from a Poisson distribution with mean 80.
- **Z** a data frame containing 5 continuous variables. Generated from a multivariate normal distribution, where the mean is calculated as  $(\gamma_i \mu_\gamma) \cdot \rho/\sigma_\gamma$  with  $\mu_\gamma = \log(4/11)$  and  $\sigma_\gamma = 0.4$ , and the correlation between covariates and provider effects is 0.1.

#### **Examples**

```
data(ExampleDataLinear)
head(ExampleDataLinear$Y)
head(ExampleDataLinear$ID)
head(ExampleDataLinear$Z)
```

linear\_fe

Main function for fitting the fixed effect linear model

#### Description

Fit a fixed effect linear model via profile likelihood or dummy encoding.

#### Usage

```
linear_fe(
  formula = NULL,
  data = NULL,
  Y = NULL,
  Z = NULL,
  ID = NULL,
  Y.char = NULL,
  Z.char = NULL,
  ID.char = NULL,
  method = "p1"
)
```

#### **Arguments**

formula

a two-sided formula object describing the model to be fitted, with the response variable on the left of a ~ operator and covariates on the right, separated by + operators. The fixed effect of the provider identifier is specified using id().

data

a data frame containing the variables named in the formula, or the columns specified by Y.char, Z.char, and ID.char.

linear\_fe 15

Υ	a numeric vector representing the response variable.
Z	a matrix or data frame representing the covariates, which can include both numeric and categorical variables.
ID	a numeric vector representing the provider identifier.
Y.char	a character string specifying the column name of the response variable in the data.
Z.char	a character vector specifying the column names of the covariates in the data.
ID.char	a character string specifying the column name of the provider identifier in the data.
method	a character string specifying the method to fit the model.

- "pl" (default) uses profile likelihood to fit the model.
- "dummy" calls 1m to fit the model using dummy variables for the provider identifier.

#### **Details**

This function is used to fit a fixed effect linear model of the form:

$$Y_{ij} = \gamma_i + \mathbf{Z}_{ij}^{\top} \boldsymbol{\beta} + \epsilon_{ij}$$

where  $Y_{ij}$  is the continuous outcome for individual j in provider i,  $\gamma_i$  is the provider-specific effect,  $\mathbf{Z}_{ij}$  are the covariates, and  $\boldsymbol{\beta}$  is the vector of coefficients for the covariates. The default method for fitting the model is profile likelihood, but dummy encoding can also be used by specifying the appropriate method. When the number of providers is very large, we recommend using the profile likelihood method, as it is computationally efficient and requires less memory usage.

The function accepts three different input formats: a formula and dataset, where the formula is of the form response  $\sim$  covariates + id(provider), with provider representing the provider identifier; a dataset along with the column names of the response, covariates, and provider identifier; or the outcome vector  $\mathbf{Y}$ , the covariate matrix or data frame  $\mathbf{Z}$ , and the provider identifier vector.

If issues arise during model fitting, consider using the data\_check function to perform a data quality check, which can help identify missing values, low variation in covariates, high-pairwise correlation, and multicollinearity. For datasets with missing values, this function automatically removes observations (rows) with any missing values before fitting the model.

#### Value

A list of objects with S3 class "linear\_fe":

coefficient	a list containing the estimated coefficients: beta, the fixed effects for each predictor, and gamma, the effect for each provider.
variance	a list containing the variance estimates: beta, the variance-covariance matrix of the predictor coefficients, and gamma, the variance of the provider effects.
sigma	the residual standard error.
fitted	the fitted values of each individual.
observation	the original response of each individual.

linear\_fe

residuals the residuals of each individual, that is response minus fitted values.

linear\_pred the linear predictor of each individual.

data\_include the data used to fit the model, sorted by the provider identifier. For categorical

covariates, this includes the dummy variables created for all categories except

the reference level.

char\_list a list of the character vectors representing the column names for the response

variable, covariates, and provider identifier. For categorical variables, the names

reflect the dummy variables created for each category.

method the method used for model fitting, either "Profile Likelihood" or "Dummy".

Loglkd log likelihood.

AIC Akaike information criterion.

BIC Bayesian information criterion.

#### References

Hsiao, C. (2022). Analysis of panel data (No. 64). Cambridge university press.

R Core Team (2023). *The R Stats Package: lm*. Available at: https://stat.ethz.ch/R-manual/R-devel/library/stats/html/lm.html

#### See Also

data\_check

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
data <- data.frame(outcome, ID, covar)
covar.char <- colnames(covar)
outcome.char <- colnames(data)[1]
ID.char <- colnames(data)[2]
formula <- as.formula(paste("outcome ~", paste(covar.char, collapse = " + "), "+ id(ID)"))
# Fit fixed linear effect model using three input formats
fit_fe1 <- linear_fe(Y = outcome, Z = covar, ID = ID)
fit_fe2 <- linear_fe(data = data, Y.char = outcome.char, Z.char = covar.char, ID.char = ID.char)
fit_fe3 <- linear_fe(formula, data)</pre>
```

linear\_re 17

linear\_re

Main Function for fitting the random effect linear model

# Description

Fit a random effect linear model via 1mer from the 1me4 package.

# Usage

```
linear_re(
  formula = NULL,
  data = NULL,
  Y = NULL,
  Z = NULL,
  ID = NULL,
  Y.char = NULL,
  Z.char = NULL,
  ID.char = NULL,
  ...
)
```

# **Arguments**

formula	a two-sided formula object describing the model to be fitted, with the response variable on the left of a $\sim$ operator and covariates on the right, separated by + operators. The random effect of the provider identifier is specified using (1   ).
data	a data frame containing the variables named in the formula, or the columns specified by Y. char, Z. char, and ID. char.
Υ	a numeric vector representing the response variable.
Z	a matrix or data frame representing the covariates, which can include both numeric and categorical variables.
ID	a numeric vector representing the provider identifier.
Y.char	a character string specifying the column name of the response variable in the data.
Z.char	a character vector specifying the column names of the covariates in the data.
ID.char	a character string specifying the column name of the provider identifier in the data.
	additional arguments passed to lmer for further customization.

## **Details**

This function is used to fit a random effect linear model of the form:

$$Y_{ij} = \mu + \alpha_i + \mathbf{Z}_{ij}^{\top} \boldsymbol{\beta} + \epsilon_{ij}$$

18 linear\_re

where  $Y_{ij}$  is the continuous outcome for individual j in provider i,  $\mu$  is the overall intercept,  $\alpha_i$  is the random effect for provider i,  $\mathbf{Z}_{ij}$  are the covariates, and  $\boldsymbol{\beta}$  is the vector of coefficients for the covariates.

The model is fitted by overloading the lmer function from the lme4 package. Three different input formats are accepted: a formula and dataset, where the formula is of the form response  $\sim$  covariates + (1 | provider), with provider representing the provider identifier; a dataset along with the column names of the response, covariates, and provider identifier; or the outcome vector Y, the covariate matrix or data frame Z, and the provider identifier vector.

In addition to these input formats, all arguments from the lmer function can be modified via ..., allowing for customization of model fitting options such as controlling the optimization method or adjusting convergence criteria. By default, the model is fitted using REML (restricted maximum likelihood).

If issues arise during model fitting, consider using the data\_check function to perform a data quality check, which can help identify missing values, low variation in covariates, high-pairwise correlation, and multicollinearity. For datasets with missing values, this function automatically removes observations (rows) with any missing values before fitting the model.

#### Value

A list of objects with S3 class "random\_re":

coefficient a list containing the estimated coefficients: FE, the fixed effects for each predic-

tor and the intercept, and RE, the random effects for each provider.

variance a list containing the variance estimates: FE, the variance-covariance matrix of

the fixed effect coefficients, and RE, the variance of the random effects.

sigma the residual standard error.

fitted the fitted values of each individual.

observation the original response of each individual.

residuals the residuals of each individual, that is response minus fitted values.

linear\_pred the linear predictor of each individual.

data\_include the data used to fit the model, sorted by the provider identifier. For categorical

covariates, this includes the dummy variables created for all categories except

the reference level.

char\_list a list of the character vectors representing the column names for the response

variable, covariates, and provider identifier. For categorical variables, the names

reflect the dummy variables created for each category.

Loglkd the log-likelihood.

AIC Akaike information criterion.

BIC Bayesian information criterion.

#### References

Bates D, Maechler M, Bolker B, Walker S (2015). *Fitting Linear Mixed-Effects Models Using lme4*. Journal of Statistical Software, 67(1), 1-48.

#### See Also

data\_check

#### **Examples**

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
data <- data.frame(outcome, ID, covar)
covar.char <- colnames(covar)
outcome.char <- colnames(data)[1]
ID.char <- colnames(data)[2]
formula <- as.formula(paste("outcome ~", paste(covar.char, collapse = " + "), "+ (1|ID)"))
# Fit random effect linear model using three input formats
fit_re1 <- linear_re(Y = outcome, Z = covar, ID = ID)
fit_re2 <- linear_re(data = data, Y.char = outcome.char, Z.char = covar.char, ID.char = ID.char)
fit_re3 <- linear_re(formula, data)</pre>
```

logis\_fe

Main function for fitting the fixed effect logistic model

# **Description**

Fit a fixed effect logistic model via Serial blockwise inversion Newton (SerBIN) or block ascent Newton (BAN) algorithm.

```
logis_fe(
  formula = NULL,
 data = NULL,
 Y.char = NULL,
 Z.char = NULL,
 ID.char = NULL,
 Y = NULL,
  Z = NULL,
  ID = NULL,
 method = "SerBIN",
 max.iter = 1000,
  tol = 1e-05,
  bound = 10,
  cutoff = 10,
  backtrack = TRUE,
  stop = "or",
  threads = 1,
```

```
message = TRUE
)
```

#### **Arguments**

formula a two-sided formula object describing the model to be fitted, with the response

variable on the left of a ~ operator and covariates on the right, separated by + operators. The fixed effect of the provider identifier is specified using id().

data a data frame containing the variables named in the formula, or the columns

specified by Y. char, Z. char, and ID. char.

Y.char a character string specifying the column name of the response variable in the

data.

Z.char a character vector specifying the column names of the covariates in the data.

ID.char a character string specifying the column name of the provider identifier in the

data.

Υ a numeric vector representing the response variable.

Ζ a matrix or data frame representing the covariates, which can include both nu-

meric and categorical variables.

ΙD a numeric vector representing the provider identifier.

a string specifying the algorithm to be used. The default value is "SerBIN". method

> • "SerBIN" uses the Serial blockwise inversion Newton algorithm to fit the model (See Wu et al. (2022)).

> • "BAN" uses the block ascent Newton algorithm to fit the model (See He et al. (2013)).

max.iter maximum iteration number if the stopping criterion specified by stop is not satisfied. The default value is 10,000.

tolerance used for stopping the algorithm. See details in stop below. The default

value is 1e-5. a positive number to avoid inflation of provider effects. The default value is 10.

bound An integer specifying the minimum number of observations required for providers. Providers with fewer observations than the cutoff will be labeled as "include =

backtrack a Boolean indicating whether backtracking line search is implemented. The default is FALSE.

a character string specifying the stopping rule to determine convergence.

0" and excluded from model fitting. The default is 10.

- "beta" stop the algorithm when the infinity norm of the difference between current and previous beta coefficients is less than the tol.
- "relch" stop the algorithm when the (loglik(m) loglik(m-1))/(loglik(m))(the difference between the log-likelihood of the current iteration and the previous iteration divided by the log-likelihood of the current iteration) is less than the tol.
- "ratch" stop the algorithm when (loglik(m) loglik(m-1))/(loglik(m) log lik(0)) (the difference between the log-likelihood of the current iteration and the previous iteration divided by the difference of the log-likelihood of the current iteration and the initial iteration) is less than the tol.

tol

cutoff

stop

 "all" stop the algorithm when all the stopping rules ("beta", "relch", "ratch") are met.

• "or" stop the algorithm if any one of the rules ("beta", "relch", "ratch") is met

The default value is or. If iter.max is achieved, it overrides any stop rule for algorithm termination.

threads a positive integer specifying the number of threads to be used. The default value

is 1.

message a Boolean indicating whether to print the progress of the fitting process. The

default is TRUE.

#### **Details**

The function accepts three different input formats: a formula and dataset, where the formula is of the form response  $\sim$  covariates + id(provider), with provider representing the provider identifier; a dataset along with the column names of the response, covariates, and provider identifier; or the binary outcome vector Y, the covariate matrix or data frame Z, and the provider identifier vector.

The default algorithm is based on Serial blockwise inversion Newton (SerBIN) proposed by Wu et al. (2022), but users can also choose to use the block ascent Newton (BAN) algorithm proposed by He et al. (2013) to fit the model. Both methodologies build upon the Newton-Raphson method, yet SerBIN simultaneously updates both the provider effect and covariate coefficient. This concurrent update necessitates the inversion of the whole information matrix at each iteration. In contrast, BAN adopts a two-layer updating approach, where the covariate coefficient is sequentially fixed to update the provider effect, followed by fixing the provider effect to update the covariate coefficient.

We suggest using the default "SerBIN" option as it typically converges subsequently much faster for most datasets. However, in rare cases where the SerBIN algorithm encounters second-order derivative irreversibility leading to an error, users can consider using the "BAN" option as an alternative. For a deeper understanding, please consult the original article for detailed insights.

If issues arise during model fitting, consider using the data\_check function to perform a data quality check, which can help identify missing values, low variation in covariates, high-pairwise correlation, and multicollinearity. For datasets with missing values, this function automatically removes observations (rows) with any missing values before fitting the model.

#### Value

A list of objects with S3 class "logis\_fe":

coefficient a list containing the estimated coefficients: beta, the fixed effects for each pre-

dictor, and gamma, the effect for each provider.

variance a list containing the variance estimates: beta, the variance-covariance matrix of

the predictor coefficients, and gamma, the variance of the provider effects.

linear\_pred the linear predictor of each individual.

prediction predicted probability of each individual
observation the original response of each individual.

Loglkd the log-likelihood.

AIC Akaike info criterion.

BIC Bayesian info criterion.

AUC area under the ROC curve.

char\_list a list of the character vectors representing the column names for the response

variable, covariates, and provider identifier. For categorical variables, the names

reflect the dummy variables created for each category.

data\_include the data used to fit the model, sorted by the provider identifier. For categorical

covariates, this includes the dummy variables created for all categories except the reference level. Additionally, it contains three extra columns: included, indicating whether the provider is included based on the cutoff argument; all.events, indicating if all observations in the provider are 1; no.events,

indicating if all observations in the provider are 0.

#### References

He K, Kalbfleisch, J, Li, Y, and et al. (2013) Evaluating hospital readmission rates in dialysis providers; adjusting for hospital effects. *Lifetime Data Analysis*, **19**: 490-512.

Wu, W, Yang, Y, Kang, J, He, K. (2022) Improving large-scale estimation and inference for profiling health care providers. *Statistics in Medicine*, **41(15)**: 2840-2853.

#### See Also

data\_check

```
data(ExampleDataBinary)
outcome <- ExampleDataBinary$Y
covar <- ExampleDataBinary$Z
ID <- ExampleDataBinary$ID
data <- data.frame(outcome, ID, covar)
covar.char <- colnames(covar)
outcome.char <- colnames(data)[1]
ID.char <- colnames(data)[2]
formula <- as.formula(paste("outcome ~", paste(covar.char, collapse = " + "), "+ id(ID)"))
# Fit logistic linear effect model using three input formats
fit_fe1 <- logis_fe(Y = outcome, Z = covar, ID = ID)
fit_fe2 <- logis_fe(data = data, Y.char = outcome.char, Z.char = covar.char, ID.char = ID.char)
fit_fe3 <- logis_fe(formula, data)</pre>
```

plot.linear\_fe 23

plot.linear_fe	Get funnel plot from a fitted linear_fe object for institutional comparisons
----------------	--

### Description

Creates a funnel plot from a linear fixed effect model to compare provider performance.

#### **Usage**

```
## S3 method for class 'linear_fe'
plot(
    x,
    null = "median",
    target = 0,
    alpha = 0.05,
    labels = c("lower", "expected", "higher"),
    point_colors = c("#E69F00", "#56B4E9", "#009E73"),
    point_shapes = c(15, 17, 19),
    point_size = 2,
    point_alpha = 0.8,
    line_size = 0.8,
    target_line_type = "longdash",
    ...
)
```

# Arguments

```
a model fitted from linear_fe.
                   a character string or a number specifying null hypotheses of fixed provider ef-
null
                   fects. The default is "median".
target
                   a numeric value representing the target outcome. The default value is 0.
alpha
                   a number or a vector of significance levels. The default is 0.05.
labels
                   a vector of labels for the plot.
point_colors
                   a vector of colors representing different provider flags. The default is c("#E69F00",
                   "#56B4E9", "#009E73").
                   a vector of shapes representing different provider flags. The default is c(15,
point_shapes
                   17, 19).
                   size of the points. The default is 2.
point_size
point_alpha
                   transparency level of the points. The default is 0.8.
line_size
                   size of all lines, including control limits and the target line. The default is 0.8.
target_line_type
                   line type for the target line. The default is "longdash".
                   additional arguments that can be passed to the function.
```

plot.logis\_fe

#### **Details**

This function generates a funnel plot from a linear fixed effect model. Currently, it only supports the indirect standardized difference. The parameter alpha is a vector used to calculate control limits at different significance levels. The first value in the vector is used as the significance level for flagging each provider, utilizing the test.linear\_fe function.

#### Value

A ggplot object representing the funnel plot.

#### See Also

```
linear_fe, linear_fe
```

#### **Examples**

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_fe <- linear_fe(Y = outcome, Z = covar, ID = ID)
plot(fit_fe)</pre>
```

plot.logis\_fe

Get funnel plot from a fitted logis\_fe object for institutional comparisons

#### **Description**

Creates a funnel plot from a logistic fixed effect model to compare provider performance.

```
## S3 method for class 'logis_fe'
plot(
    X,
    null = "median",
    test = "score",
    target = 1,
    alpha = 0.05,
    labels = c("lower", "expected", "higher"),
    point_colors = c("#E69F00", "#56B4E9", "#009E73"),
    point_shapes = c(15, 17, 19),
    point_size = 2,
    point_alpha = 0.8,
    line_size = 0.8,
    target_line_type = "longdash",
```

plot.logis\_fe 25

```
)
```

#### **Arguments**

	x	a model fitted from logis_fe.
	null	a character string or a number specifying null hypotheses of fixed provider effects. The default is "median".
	test	a character string specifying the type of testing methods to be conducted. The default is "score".
	target	a numeric value representing the target outcome. The default value is 1.
	alpha	a number or a vector of significance levels. The default is 0.05.
	labels	a vector of labels for the plot.
	point_colors	a vector of colors representing different provider flags. The default is $c("\#E69F00", "\#56B4E9", "\#009E73")$ .
	point_shapes	a vector of shapes representing different provider flags. The default is $c(15, 17, 19)$ .
	point_size	size of the points. The default is 2.
	point_alpha	transparency level of the points. The default is 0.8.
	line_size	size of all lines, including control limits and the target line. The default is 0.8.
<pre>target_line_type</pre>		
		line type for the target line. The default is "longdash".

#### **Details**

This function generates a funnel plot from a logistic fixed-effect model. Currently, it only supports the indirect standardized ratio. The parameter alpha is a vector used to calculate control limits at different significance levels. The first value in the vector is used as the significance level for flagging each provider, utilizing the test.logis\_fe function.

additional arguments that can be passed to the function.

# Value

A ggplot object representing the funnel plot.

#### References

Wu, W., Kuriakose, J. P., Weng, W., Burney, R. E., & He, K. (2023). Test-specific funnel plots for healthcare provider profiling leveraging individual- and summary-level information. *Health Services and Outcomes Research Methodology*, **23(1)**, 45-58.

#### See Also

```
logis_fe, SM_output.linear_re, test.logis_fe
```

SM\_output.linear\_fe

#### **Examples**

```
data(ExampleDataBinary)
outcome <- ExampleDataBinary$Y
covar <- ExampleDataBinary$Z
ID <- ExampleDataBinary$ID
fit_fe <- logis_fe(Y = outcome, Z = covar, ID = ID)
plot(fit_fe)</pre>
```

SM\_output

Generic function for calculating standardized measures

#### **Description**

SM\_output is an S3 generic function designed to calculate standardized measures. It dispatches to the appropriate method based on the class of the input (fit), ensuring the correct method is applied for different types of models.

#### Usage

```
SM_output(fit, ...)
```

#### **Arguments**

fit the input object, typically a fitted model, for which standardized measures are calculated. The method applied depends on the class of this object.

... additional arguments that can be passed to specific methods.

#### Value

the return varies depending on the method implemented for the class of the input object.

```
{\tt SM\_output.linear\_fe} \qquad {\it Calculate \ direct/indirect \ standardized \ differences \ from \ a \ fitted} \\ {\tt linear\_fe \ object}
```

# **Description**

Provide direct/indirect standardized differences for a fixed effect linear model.

```
## S3 method for class 'linear_fe'
SM_output(fit, parm, stdz = "indirect", null = "median", ...)
```

SM\_output.linear\_fe 27

#### **Arguments**

stdz

fit a model fitted from linear\_fe.

parm specifies a subset of providers for which confidence intervals are to be given. By default, all providers are included. The class of parm should match the class of the provider IDs.

a character string or a vector specifying the standar

a character string or a vector specifying the standardization method(s). The possible values are:

- "indirect" (default) indirect standardization method.
- "direct" direct standardization method.
- c("indirect", "direct") outputs both direct and indirect standardized measures.

null a character string or a number defining the population norm. The default value is "median". The possible values are:

- "median" the median of the provider effect estimates  $(\hat{\gamma}_i)$ .
- "mean" the weighted average of the provider effect estimates  $(\hat{\gamma}_i)$ , where the weights correspond to the sample size of each provider.
- numeric a user-defined numeric value representing the population norm.

additional arguments that can be passed to the function.

#### **Details**

This function computes standardized differences for a fixed effect linear model using either direct or indirect methods, or both when specified. For each method, the population norm is determined by the null argument. The population norm can be the median of the estimates, their weighted mean (with weights corresponding to provider sizes), or a user-defined numeric value.

#### Value

A list containing the standardized differences based on the method(s) specified in stdz, as well as the observed and expected outcomes used to calculate the standardized measures:

indirect.difference

indirect standardized differences, if stdz includes "indirect".

direct.difference

direct standardized differences, if stdz includes "direct".

OE a list of data frames containing the observed and expected outcomes used for calculating standardized measures.

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_linear <- linear_fe(Y = outcome, Z = covar, ID = ID)
SM_output(fit_linear)
SM_output(fit_linear, stdz = "direct", null = "mean")</pre>
```

28 SM\_output.linear\_re

SM\_output.linear\_re Calculate direct/indirect standardized differences from a fitted linear\_re object

#### **Description**

Provide direct/indirect standardized differences for a random effect linear model.

### Usage

```
## S3 method for class 'linear_re'
SM_output(fit, parm, stdz = "indirect", ...)
```

#### **Arguments**

fit a model fitted from linear\_re.

parm specifies a subset of providers for which confidence intervals are to be given. By default, all providers are included. The class of parm should match the class of the provider IDs.

stdz a character string or a vector specifying the standardization method(s). The possible values are:

- "indirect" (default) indirect standardization method.
- "direct" direct standardization method.
- c("indirect", "direct") outputs both direct and indirect standardized measures.

. . . additional arguments that can be passed to the function.

#### **Details**

This function computes standardized differences for a random effect linear model using either direct or indirect methods, or both when specified. The function returns both the standardized differences and the observed and expected outcomes used for their calculation.

#### Value

A list containing the standardized differences based on the method(s) specified in stdz, as well as the observed and expected outcomes used to calculate the standardized measures:

SM\_output.logis\_fe 29

#### **Examples**

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_linear <- linear_re(Y = outcome, Z = covar, ID = ID)
SM_output(fit_linear)</pre>
```

 ${\tt SM\_output.logis\_fe}$ 

Calculate direct/indirect standardized ratios/rates from a fitted logis\_fe object

#### **Description**

Provide direct/indirect standardized ratios/rates for a fixed effect logistic model.

#### Usage

```
## $3 method for class 'logis_fe'
$M_output(
    fit,
    parm,
    stdz = "indirect",
    measure = c("rate", "ratio"),
    null = "median",
    threads = 2,
    ...
)
```

#### **Arguments**

fit

a model fitted from logis\_fe.

parm

specifies a subset of providers for which confidence intervals are to be given. By default, all providers are included. The class of parm should match the class of the provider IDs.

stdz

a character string or a vector specifying the standardization method(s). The possible values are:

- "indirect" (default) indirect standardization method.
- "direct" direct standardization method.
- c("indirect", "direct") outputs both direct and indirect standardized measures.

measure

a character string or a vector indicating whether the output measure is "ratio" or "rate"

• "rate" output the standardized rate. The "rate" has been restricted to 0% - 100%.

30 SM\_output.logis\_fe

• "ratio" output the standardized ratio.

• c("ratio", "rate") (default) output both the ratio and rate.

null if "stdz = indirect", a character string or a number defining the population

norm. The default is "median".

threads an integer specifying the number of threads to use. The default value is 2.

... additional arguments that can be passed to the function.

#### Value

A list contains standardized measures, as well as the observed and expected outcomes used for calculation, depending on the user's choice of standardization method (stdz) and measure type (measure).

indirect.ratio standardization ratio using indirect method if stdz includes "indirect" and

measure includes "ratio".

direct.ratio standardization ratio using direct method if stdz includes "direct" and measure

includes "ratio".

indirect.rate standardization rate using indirect method if stdz includes "indirect" and

measure includes "rate".

direct.rate standardization rate using direct method if stdz includes "direct" and measure

includes "rate".

OE a list of data frames containing the observed and expected outcomes used for

calculating standardized measures.

#### References

He, K. (2019). Indirect and direct standardization for evaluating transplant centers. *Journal of Hospital Administration*, **8(1)**, 9-14.

```
data(ExampleDataBinary)
outcome = ExampleDataBinary$Y
covar = ExampleDataBinary$Z
ID = ExampleDataBinary$ID
fit_fe <- logis_fe(Y = outcome, Z = covar, ID = ID, message = FALSE)
SR <- SM_output(fit_fe, stdz = "direct", measure = "rate")
SR$direct.rate</pre>
```

summary.linear\_fe 31

summary.linear_fe	Result Summaries of Covariate Estimates from a fitted linear_fe or linear_re object

# Description

Provide the summary statistics for the covariate estimates for a fixed/random effect linear model.

### Usage

```
## S3 method for class 'linear_fe'
summary(object, parm, level = 0.95, null = 0, alternative = "two.sided", ...)
## S3 method for class 'linear_re'
summary(object, parm, level = 0.95, null = 0, alternative = "two.sided", ...)
```

# **Arguments**

object	a model fitted from linear_fe or linear_re.
parm	Specifies a subset of covariates for which the result summaries should be output. By default, all covariates are included.
level	the confidence level during the hypothesis test, meaning a significance level of $1-$ level. The default value is $0.95.$
null	a number defining the null hypothesis for the covariate estimates. The default value is $\emptyset$ .
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater", or "less".
	additional arguments that can be passed to the function.

#### Value

A data frame containing summary statistics for covariate estimates, with the following columns:

Estimate	the estimates of covariate coefficients.
Std.Error	the standard error of the estimate.
Stat	the test statistic.
p value	the p-value for the hypothesis test.
CI.upper	the lower bound of the confidence interval.
CI.lower	the upper bound of the confidence interval.

32 summary.logis\_fe

#### **Examples**

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_fe <- linear_fe(Y = outcome, Z = covar, ID = ID)
summary(fit_fe)

data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_re <- linear_fe(Y = outcome, Z = covar, ID = ID)
summary(fit_re)</pre>
```

summary.logis\_fe

Result Summaries of Covariate Estimates from a fitted logis\_fe object

# **Description**

Provide the summary statistics for the covariate estimates for a fixed effect logistic model.

#### Usage

```
## $3 method for class 'logis_fe'
summary(
   object,
   parm,
   level = 0.95,
   test = "wald",
   null = 0,
   alternative = "two.sided",
   ...
)
```

#### **Arguments**

object a model fitted from logis\_fe.

Specifies a subset of covariates for which the result summaries should be output. By default, all covariates are included.

level the confidence level during the hypothesis test, meaning a significance level of 1 - level. The default value is 0.95.

test a character string specifying the type of testing method. The default is "wald".

• "wald" wald test.

test 33

• "lr"likelihood ratio test.

• "score"score test.

null a number defining the null hypothesis for the covariate estimates. The default

value is 0.

alternative a character string specifying the alternative hypothesis when test = "wald",

must be one of "two.sided" (default), "greater", or "less".

. . . additional arguments that can be passed to the function.

#### Value

A data frame containing summary statistics for covariate estimates, with the following columns:

Estimate the estimates of covariate coefficients.

Std.Error the standard error of the estimate, included only when test = "wald".

Stat the test statistic.

p value the p-value for the hypothesis test.

CI.upper the lower bound of the confidence interval, included only when test = "wald".

CI.lower the upper bound of the confidence interval, included only when test = "wald".

#### **Examples**

```
data(ExampleDataBinary)
outcome = ExampleDataBinary$Y
covar = ExampleDataBinary$Z
ID = ExampleDataBinary$ID

fit_fe <- logis_fe(Y = outcome, Z = covar, ID = ID, message = FALSE)
summary.wald <- summary(fit_fe, level = 0.95, test = "wald")
summary.wald</pre>
```

test

Generic function for hypothesis testing of provider effects

#### **Description**

test is an S3 generic function used to conduct hypothesis tests on provider effect coefficients and detect outlying provider. The function dispatches to the appropriate method based on the class of the input model (fit).

```
test(fit, ...)
```

34 test.linear\_fe

# **Arguments**

fit	the input object, typically a fitted model, for which provider effects are tested. The method applied depends on the class of this object.
	additional arguments that can be passed to specific methods.

### Value

the return depends on the method implemented for the class of the input object, typically including statistical outputs for provider effect coefficients and identification of outlier providers.

test.linear_fe	Conduct hypothesis testing for provider effects from a fitted linear_fe object	
----------------	--	--

# Description

Conduct hypothesis tests on provider effects and identify outlying providers for a fixed effect linear model.

### Usage

```
## S3 method for class 'linear_fe'
test(fit, parm, level = 0.95, null = "median", alternative = "two.sided", ...)
```

# Arguments

fit	a model fitted from linear_fe.
parm	specifies a subset of providers for which confidence intervals are to be given. By default, all providers are included. The class of parm should match the class of the provider IDs.
level	the confidence level during the hypothesis test, meaning a significance level of $1-$ level. The default value is $0.95$ .
null	a character string or a number defining the null hypothesis for the provider effects. The default value is "median". The possible values are:
	<ul> <li>"median": The median of the provider effect estimates (γ̂<sub>i</sub>).</li> <li>"mean": The weighted average of the provider effect estimates (γ̂<sub>i</sub>), where the weights correspond to the sample size of each provider.</li> <li>numeric: A user-defined numeric value representing the null hypothesis.</li> </ul>
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater", or "less".
	additional arguments that can be passed to the function.

test.linear\_re 35

#### **Details**

The function identifies outlying providers based on hypothesis test results. For two-sided tests, 1 indicates performance significantly higher than expected,  $\neg 1$  indicates lower, For one-sided tests, 1 (right-tailed) or  $\neg 1$  (left-tailed) flags are used. Providers whose performance falls within the central range are flagged as  $\emptyset$ . Outlying providers are determined by the test statistic falling beyond the threshold based on the significance level 1 — level.

#### Value

A data frame containing the results of the hypothesis test, with the following columns:

flag a flagging indicator where 1 means statistically higher than expected and -1

means statistically lower than expected.

p-value the p-value of the hypothesis test.

stat the test statistic.

Std. Error the standard error of the provider effect estimate.

#### **Examples**

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
covar <- ExampleDataLinear$Z
ID <- ExampleDataLinear$ID
fit_linear <- linear_fe(Y = outcome, Z = covar, ID = ID)
test(fit_linear)</pre>
```

```
test.linear_re Conduct hypothesis testing for provider effects from a fitted linear_re object
```

# Description

Conduct hypothesis tests on provider effects and identify outlying providers for a random effect linear model.

```
## S3 method for class 'linear_re'
test(fit, parm, level = 0.95, null = 0, alternative = "two.sided", ...)
```

36 test.linear\_re

#### **Arguments**

fit a model fitted from linear\_re.

parm specifies a subset of providers for which confidence intervals are to be given. By

default, all providers are included. The class of parm should match the class of

the provider IDs.

level the confidence level during the hypothesis test, meaning a significance level of

1 -level. The default value is 0.95.

null a number defining the null hypothesis for the provider effects. The default value

is 0.

alternative a character string specifying the alternative hypothesis, must be one of "two.sided"

(default), "greater", or "less".

. . . additional arguments that can be passed to the function.

#### **Details**

The function identifies outlying providers based on hypothesis test results. For two-sided tests, 1 indicates performance significantly higher than expected, -1 indicates lower, For one-sided tests, 1 (right-tailed) or -1 (left-tailed) flags are used. Providers whose performance falls within the central range are flagged as  $\emptyset$ . Outlying providers are determined by the test statistic falling beyond the threshold based on the significance level 1 — level.

## Value

A data frame containing the results of the hypothesis test, with the following columns:

flag a flagging indicator where 1 means statistically higher than expected and -1

means statistically lower than expected.

p-value the p-value of the hypothesis test.

stat the test statistic.

Std. Error the standard error of the provider effect estimate.

```
data(ExampleDataLinear)
outcome <- ExampleDataLinear$Y
ID <- ExampleDataLinear$ID
covar <- ExampleDataLinear$Z
fit_re <- linear_re(Y = outcome, Z = covar, ID = ID)
test(fit_re)</pre>
```

test.logis\_fe 37

test.logis_fe	Conduct hypothesis testing for provider effects from a fitted logis_fe
	object

### Description

Conduct hypothesis tests on provider effects and identify outlying providers for a fixed effect logistic model.

#### Usage

```
## S3 method for class 'logis_fe'
test(
  fit,
  parm,
  level = 0.95,
  test = "exact.poisbinom",
  score_modified = TRUE,
 null = "median",
  n = 10000,
  threads = 1,
  alternative = "two.sided",
)
```

# **Arguments**

fit	a model fitted from logis_fe.
parm	specifies a subset of providers for which confidence inte

tervals are to be given. By default, all providers are included. The class of parm should match the class of the provider IDs.

the confidence level during the hypothesis test, meaning a significance level of 1 -level. The default value is 0.95.

> a character string specifying the type of testing method to be conducted. The default is "exact.poisbinom".

- "exact.poisbinom" exact test based on Poisson-binomial distribution of  $O_i|Z_i$ .
- "exact.bootstrap" exact test based on bootstrap procedure.
- · "wald" wald test.
- "score"score test.

score\_modified a logical indicating whether to use the modified score test ignoring the randomness of covariate coefficient for score teat ("test = score"). The default value

is TRUE.

a character string or a number specifying null hypotheses of fixed provider effects. The default is "median".

level test

null

38 test.logis\_fe

n resample size for bootstrapping when ("test = exact.bootstrap"). The de-

fault value is 10,000.

threads an integer specifying the number of threads to use. The default value is 1.

alternative a character string specifying the alternative hypothesis, must be one of "two.sided"

(default), "greater", or "less".

... additional arguments that can be passed to the function.

#### **Details**

By default, the function uses the "exact.poisbinom" method. The wald test is invalid for extreme providers (i.e. when provider effect goes to infinity). For the score test, consider that when the number of tested providers is large, refitting the models to get the restricted MLEs will take a long time. Therefore, we use unrestricted MLEs to replace the restricted MLEs during the testing procedure by default. However, the user can specify score\_modified = FALSE to perform a standard score test.

#### Value

A data frame containing the results of the hypothesis test, with the following columns:

flag a flagging indicator where 1 means statistically higher than expected and -1

means statistically lower than expected.

p-value the p-value of the hypothesis test.

stat the test statistic.

Std.Error The standard error of the provider effect estimate, included only when test =

"wald".

# References

Wu, W, Yang, Y, Kang, J, He, K. (2022) Improving large-scale estimation and inference for profiling health care providers. *Statistics in Medicine*, **41**(15): 2840-2853.

```
data(ExampleDataBinary)
outcome = ExampleDataBinary$Y
covar = ExampleDataBinary$Z
ID = ExampleDataBinary$ID
fit_fe <- logis_fe(Y = outcome, Z = covar, ID = ID, message = FALSE)
test(fit_fe, test = "score")</pre>
```

# **Index**

* (CENR)
logis_fe, 19
* Algorithm,
logis_fe, 19
* Cost-Efficient
logis_fe, 19
* Effects
logis_fe, 19
* Fixed
logis_fe, 19
* Newton-Raphson
logis_fe, 19
* Provider
logis_fe, 19
* datasets
ecls_data, 11
ExampleDataBinary, 13
ExampleDataLinear, 13
bar_plot, 2
caterpillar_plot, 4
confint.linear_fe, 5, 6
confint.linear_re, 5, 7
confint.logis_fe, 5, 9
_ , , ,
data_check, 10, 16, 19, 22
ecls_data, 11
ExampleDataBinary, 13
ExampleDataLinear, 13
linear_fe, 14, 24
linear_re, 17
lm, <i>15</i>
lmer, <i>17</i> , <i>18</i>
logis_fe, 19, 25
plot.linear_fe, 23
plot.logis_fe, 24

```
SM_output, 26
{\tt SM\_output.linear\_fe, \it 7, 26}
SM_output.linear_re, 8, 25, 28
SM_output.logis_fe, 9, 29
\verb|summary.linear_fe|, 31|
summary.linear_re(summary.linear_fe),
\verb|summary.logis_fe|, 32|
test, 33
test.linear_fe, 3, 24, 34
test.linear_re, 3, 35
test.logis_fe, 3, 25, 37
```